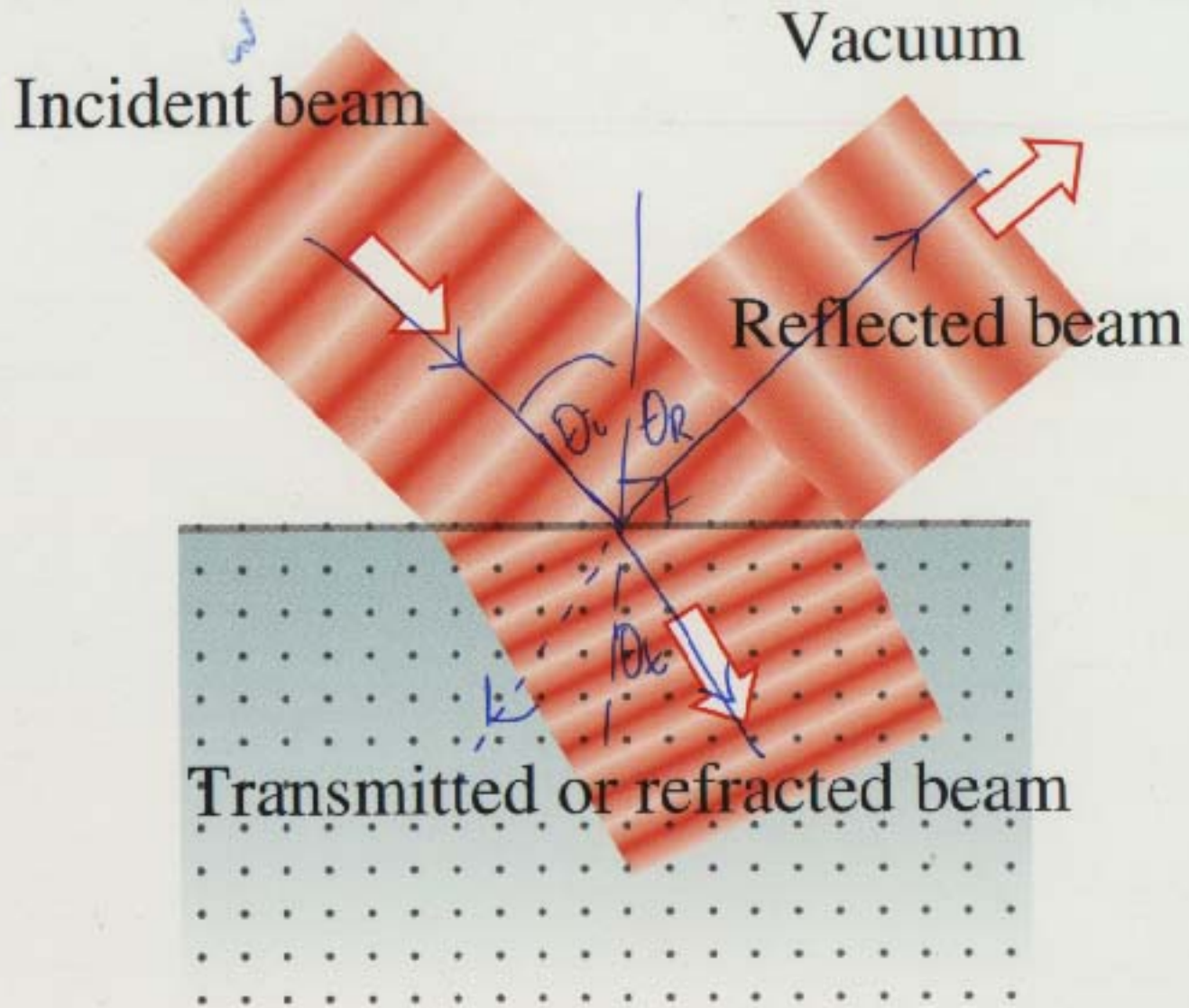


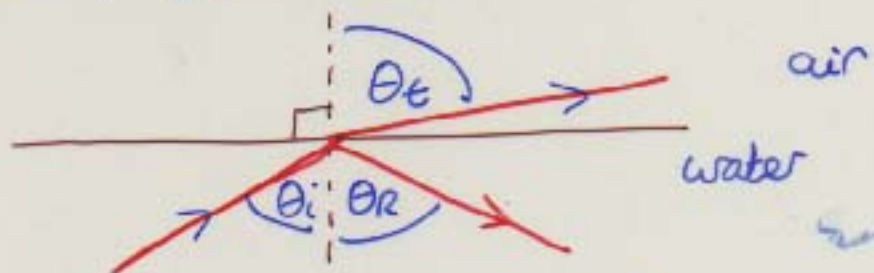
Figure 23.12  
**Reflected and transmitted light**



## Total Internal Reflection

- can occur when light beam travels from dense to less dense medium (i.e.  $n_i > n_t$ )

e.g. glass  $\rightarrow$  air, glass  $\rightarrow$  water



(Fraction of beam reflected with  $\theta_r = \theta_i$ )

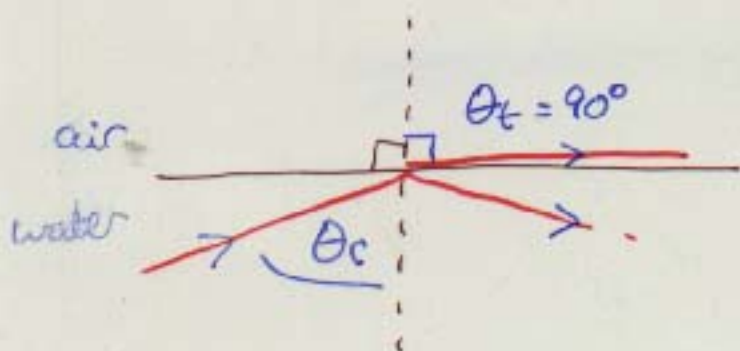
From Snell's law, refracted beam has  $\theta_t > \theta_i$   
i.e. bends away from surface normal

As  $\theta_i$  increases:

- reflected fraction increases
- refracted light has  $\sin \theta_t = \overbrace{\left(\frac{n_i}{n_t}\right)}^{>1} \sin \theta_i$

When  $\theta_i$  is such that  $\sin \theta_i = \left(\frac{n_t}{n_i}\right)$ ,  $\Rightarrow \sin \theta_t = 1$

i.e.  $\theta_t = 90^\circ$ , refracted ray skims along surface



This is the critical angle  $\theta_c$   
of incidence

$$\sin \theta_c = \left(\frac{n_t}{n_i}\right) (<1)$$

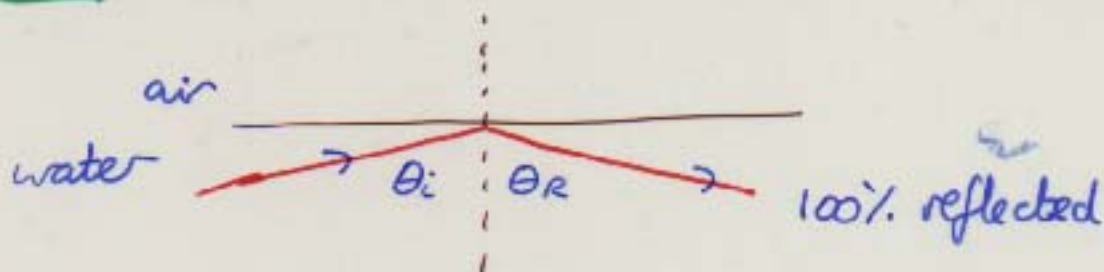


## T. I. R. cont/d

For  $\theta_i > \theta_c$ ,  $\sin \theta_t = \frac{n_i}{n_t} \sin \theta_i > 1$

i.e. no refraction possible!

So all light is reflected inside surface, cannot escape.

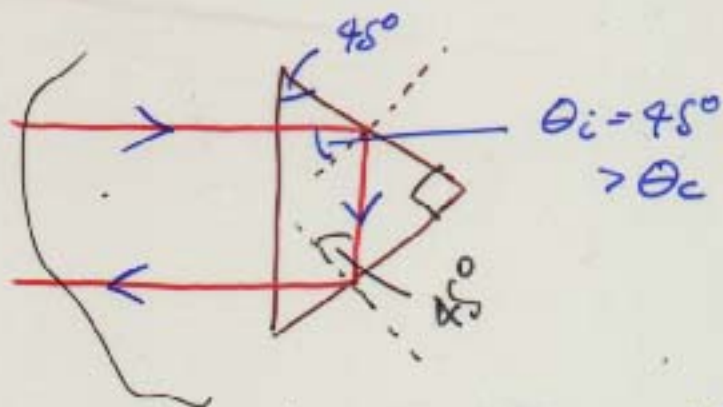


e.g. binoculars use prisms as mirrors:  $\approx 100\%$  efficient!

For glass  $\rightarrow$  air

$$n_g = 1.5, n_a = 1.00028$$

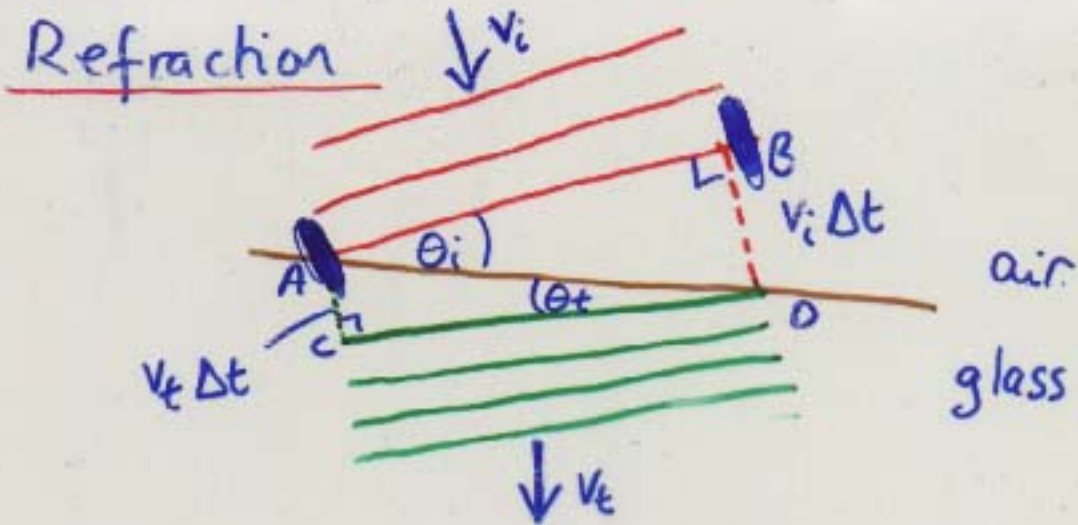
$$\Rightarrow \sin \theta_c = \frac{1}{1.5} \Rightarrow \theta_c = 41.8^\circ$$



(Note, would not work underwater! Then  $\sin \theta_c = \frac{1.33}{1.5} \frac{n_t}{n_i}$   
 $\Rightarrow \theta_c = 62^\circ$ )

c.f. diamond/air with  $n_d = 2.42 \Rightarrow \theta_c = 24.4^\circ$   
(cut facets designed to trap light inside: sparkle)

Note: If  $n_t < n_i$  or  $n_t = n_i$ , no T.I.R. can occur  
(some light always transmitted)



Across interface:

1.  $n_i \sin \theta_i = n_t \sin \theta_t$  : Snell's Law
2. Speed changes  $v = \frac{c}{n}$
3. Wavelengths  $\lambda = \frac{v}{f} \Rightarrow \underline{\lambda_i n_i = \lambda_t n_t}$

Note: "color" measures  $f$ , not  $\lambda$ , so unchanged  
 $\lambda_0 = \text{max (vacuum) wavelength}$

4. Area of beam changes:

In glass, cross-section  $CD = AD \cos \theta_t$

In air,  $AB = AD \cos \theta_i$

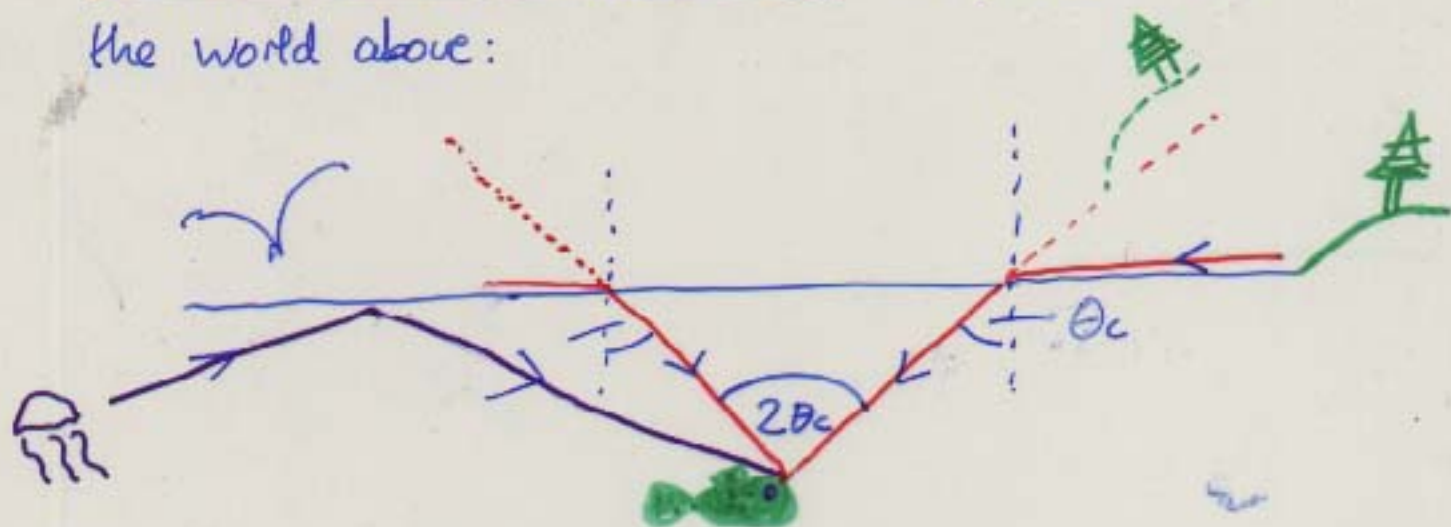
From Snell's Law,  $\theta_t < \theta_i$  so  $CD > AB$

( $\Rightarrow$  same energy spread over larger area

$\Rightarrow$  irradiance  $\downarrow$ )



Example (HW ch 23, problem 67) - A fish's view of the world above:



Objects on shore (or on surface far away) have  $\theta_{air} = 90^\circ$

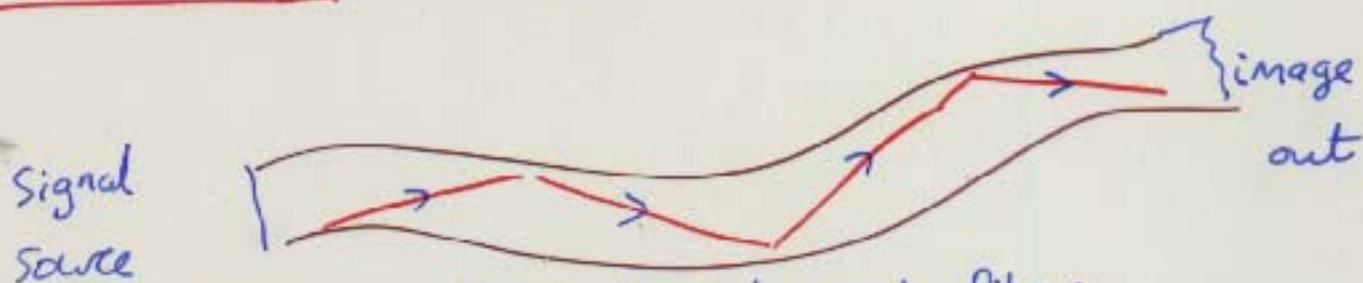
Panorama of world above lake appears in a cone

of light above fish, with cone angle  $2\theta_c$

(For water/air,  $\theta_c = \sin^{-1}\left(\frac{1}{1.33}\right) = 48.6^\circ$ )

Outside this cone, fish sees a reflection of bottom  
+ objects in water

Optical Fibers (endoscopy, cable TV/catenet)



T.I.R. keeps light trapped inside fiber

## Color (ch. 23.7)

Additive Color: can combine light beams to produce any color we can perceive

e.g. Red + Green + Blue = White  
"primary" colors

Note, e.g.  $R + G = \text{Yellow}$

eye is "fooled" by  
mixing 2 colors  $\rightarrow$  intermediate color.

Also: Red + Blue = Magenta

Blue + Green = Cyan

Red + Green = Yellow

So:

$$M + G = W$$

$$C + R = W$$

$$Y + B = W$$

"complementary" colors.

Adding additional color  $\rightarrow$  increases "white" contribution  
color becomes "unsaturated"

$$\text{e.g. } M + Y = (R+B) + (R+G)$$

$$= (R+G+B) + R$$

$$= \text{White} + \text{Red} : \text{"Pink"}$$



## "Subtractive" Color : Absorption + Reflection

- Filters can absorb certain frequencies from white light  
e.g. Yellow filter transmits  $Y = R + G$ , absorbs Blue

Adding more filters  $\rightarrow$  more colors absorbed

$\rightarrow$  Black when no light transmitted

- Dyes, pigments, inks absorb some frequencies, reflect others (e.g. red shirt absorbs  $G + B$ , reflects red)

e.g. Color printing done with Cyan, Magenta, Yellow ink  
(+ black  $\Rightarrow$  "CMYK" printing) - can produce ~ any color in reflected light.

- Reflected / filtered light only subtracts color, cannot "create" it, e.g. through blue-tinted glasses, all colors  $\rightarrow$  shades from black to bright blue
- Transparent small particles (cloud droplets, salt or sugar crystals)  
 $\Rightarrow$  diffuse reflection of all colors  
 $\Rightarrow$  reflect "white" light (or color of light source)